# ELECTRICAL & ELECTRONICS ENGINEERING

CODE	COURSE NAME	CATEGORY	L	Τ	Р	CREDIT
EET305	SIGNALS AND SYSTEMS	РСС	3	1	0	4

Preamble: This course introduces the concept of signals and systems. The time<br/>domain and frequency domain representation, operations and analysis<br/>of both the continuous time and discrete time systems are discussed.<br/>The application of Fourier analysis, Laplace Transform and Z-<br/>Transforms are included. Stability analysis of continuous time systems<br/>and discrete time systems are also introduced.

#### Prerequisite : Basics of Circuits and Networks

**Course Outcomes** : After the completion of the course the student will be able to:

CO 1	Explain the basic operations on signals and systems.
CO 2	Apply Fourier Series and Fourier Transform concepts for continuous time signals.
CO 3	Analyse the continuous time systems with Laplace Transform.
<b>CO 4</b>	Analyse the discrete time system using Z Transform.
CO 5	Apply Fourier Series and Fourier Transform concepts for Discrete time domain.
CO 6	Describe the concept of stability of continuous time systems and sampled data
	systems.

#### Mapping of course outcomes with program outcomes

	PO 1	PO 2	PO 3	<b>PO 4</b>	PO 5	PO 6	<b>PO 7</b>	PO 8	PO 9	PO 10	PO 11	PO 12
CO 1	3	3	-		2	-	-	-	-	-	-	1
CO 2	3	3	3	-	-	-	-	-	-	-	-	1
CO 3	3	3	3	-	2	-	-	-	<b>-</b> -	-	-	2
CO 4	3	3	3	-	2	-	-	-	-	-	-	2
CO 5	3	3	3	-	-//	-	-	-	-	-	-	2
CO 6	3	3	-	-	2	- 5-10	-	-	-	-	-	1

#### **Assessment Pattern:**

Total Marks	CIE marks	ESE marks	ESE Duration
150	50	100	03 Hrs

Bloom's Category	Continuous As	ssessment Tests	End Semester Examination		
8,	1	2			
Remember (K1)	10	10	20		
Understand (K2)	10	10	20		
Apply (K3)	30	30	60		
Analyse (K4)					
Evaluate (K5)					
Create (K6)					

**End Semester Examination Pattern** : There will be two parts; Part A and Part B. **Part A** contains 10 questions with 2 questions from each module, having 3 marks for each question. Students should answer all questions.

**Part B** contains 2 questions from each module of which student should answer any one. Each question carries 14 marks and can have maximum 2 sub-divisions.

# Course Level Assessment Questions :

#### **Course Outcome 1 (CO1)**

- 1. What are the standard test signals?
- 2. Problems related to various operations of signals.
- 3. Problems related to representation of systems in differential equation form.
- 4. Explain any three differences between linear and nonlinear systems.

#### Course Outcome 2 (CO2):

- 1. Problems related to Fourier series of continuous signals.
- 2. Problems related to Fourier transform of continuous systems.
- 3. Obtain the frequency response of the given system.

#### Course Outcome 3(CO3):

- 1. Derivations of transfer function of a given electrical system to comment on the system behaviour.
- 2. Problems related to analogous systems.
- 3. Problems related to block diagram reduction.

#### **Course Outcome 4 (CO4):**

- 1. Problems related ZIT.
- 2. Problems related to ZTF from difference equation form.
- 3. Problems related to block diagram development of ZTF of the given sampled system.

#### **Course Outcome 5 (CO5):**

- 1. Problems related to Discrete Fourier series of DT signals.
- 2. Problems related to Discrete time Fourier transform of DT signals
- 3. Obtain the frequency response of the given DT system.

#### Course Outcome 6 (CO6):

- 1. Problems related to the stability analysis of given continuous time systems using Routh criterion.
- 2. Problems related to stability analysis of DT systems.
- 3. Differentiate between asymptotic stability and BIBO stability?

# **Model Question Paper QPCODE:**

PAGES: 3

(7)

Reg. No: Name:

# **APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY** FIFTH SEMESTER B.TECH DEGREE EXAMINATION **MONTH & YEAR**

Course Code: EET305

# Course Name: SIGNALS AND SYSTEMS

Max. Marks: 100

#### **Duration: 3 Hours**

# PART A

Answer all Questions. Each question carries 3 Marks

- 1 Define unit ramp signal r(t). Sketch the signal r(-t+2).
- 2 Explain any two peculiar characteristics of nonlinear systems.
- What are the conditions for the existence of Fourier transform? 3
- Why do you use analogous systems? Explain with a suitable example. 4
- Determine the unit impulse response for the system with  $T(s) = \frac{2}{(s^2 + s 12)}$ 5

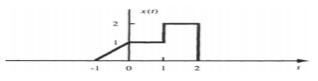
- Explain the concept of positive real functions. 6
- Explain the significance of ZOH circuit in signal reconstruction. 7
- Write three properties of discrete convolution. 8
- 9 State and prove time reversal property of discrete time Fourier series.
- Find the Fourier transform of x(n) = n u(n). 10

# PART B

# Answer any one full question from each module. Each question carries 14 Marks

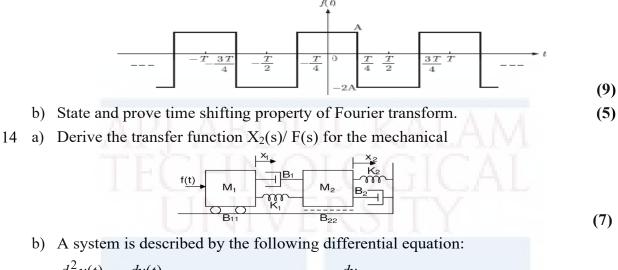
# Module 1

- a) Check whether the following system is static, causal, linear and time invariant: 11 y(t) = |x(t)|(8)
  - b) Find the convolution of  $x_1(t)$ and  $x_2(t)$ for the following signals:  $x_1(t) = e^{-at}u(t); x_2(t) = e^{-bt}u(t)$ (6)
- 12 a) With suitable examples differentiate between:
  - i. Odd and even signals,
  - ii. Causal and non causal systems.
  - b) The signal x(t) is given below. Plot x(t-1)+x(-t+2)(7)



Module 2

a) Find the trigonometric Fourier series for the periodic signal f(t). 13



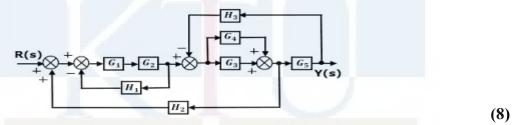
$$\frac{d^2 y(t)}{dt^2} + 7\frac{dy(t)}{dt} + 12y(t) = x(t); y(0^-) = -2, \frac{dy}{dt}(0^-) = 0$$

Determine the response of the system to a unit step applied at t=0.

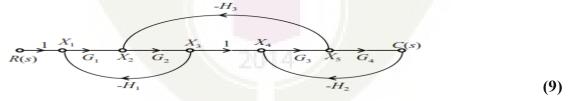
# (7)

#### Module 3

a) Determine the overall transfer function Y(s)/R(s) using block diagram reduction. 15



- b) Check stability of the system represented by the following characteristic equation, using Routh stability criterion:  $3s^4+10s^3+5s^2+5s+2=0$ (6)
- a) Determine the transfer function of the system represented by the signal flow graph 16 using Mason's gain formula.



b) How frequency response can be obtained from poles and zeros? (5)

# **Module 4**

- Determine the convolution sum of two sequences  $x(n) = \{1,4,3,2\}$ and 17 a)  $h(n) = \{1,3,2,1\}$  using graphical method. (8)
  - b) Determine the z-transform of  $x(n)=(1/2)^n u(-n)$ . (6)
- Explain the aliasing effect in sampled data systems. (5) 18 a)
  - $i) X(z) = \frac{2z^{-1}}{(1 \frac{1}{4}z^{-1})^2}; ROC: |z| > \frac{1}{4}, and, ii) F(z) = \frac{3z^{-1}}{(1 z^{-1})(1 2z^{-1})}; ROC: |z| > 2$ (9) b) Determine functions:

#### Module 5

- 19 a) Determine the complete solution of the difference equation: y(n) + 2y(n-1) + y(n-2) = x(n) + x(n-1) for the input  $x(n) = (0.5^n) u(n)$ , initial conditions y(-1) = y(-2) = 1? (9)
  - b) Find the Fourier series coefficients for  $x(n) = cos(\pi n/4)$  (5)

# 20 a) i) Obtain the direct form-I realization for the system described by the difference equation: $y(n) - \frac{5}{6}y(n-1) + \frac{1}{6}y(n-2) = 2x(n)$

ii) Also determine the impulse response h(n) for the above system. (4+5)

b) Check stability of the system described by the following characteristic equation, using Jury's test:  $z^3-0.2z^2-0.25z+0.05=0$  (5)

#### **Syllabus**

#### Module 1

#### Introduction to Signals and Systems (9 hours):

Classification of signals: Elementary signals- Basic operations on continuous time and discrete time signals

Concept of system: Classification of systems- Properties of systems- Time invariance-Linearity -Causality – Memory- Stability-Convolution Integral- Impulse response

Representation of LTI systems: Differential equation representations of LTI systems

Basics of Non linear systems- types and properties

Introduction to random signals and processes (concepts only)

#### Module 2

#### Fourier Analysis and Laplace Transform Analysis (10 hours):

Fourier analysis of continuous time signals: Fourier Series- Harmonic analysis of common signals

Fourier transform: Existence- Properties of Continuous time Fourier transform- Energy spectral density and power spectral density

Concept of Frequency response

Laplace transform analysis of system transfer function: Relation between the transfer function and differential equation- Transfer function of LTI systems- Electrical, translational and rotational mechanical systems- Force voltage, Force current and Torque Voltage analogy

#### Module 3

# System Models and Response (8 hours):

Block diagram representation - block diagram reduction

Signal flow graph - Mason's gain formula

Type and Order of the systems- Characteristic equation

Determining the time domain and frequency response from poles and zeros

Concepts of Positive real functions and Hurwitz polynomial- Routh stability criterion.

Simulation based analysis: Introduction to simulation tools like MATLAB/ SCILAB or equivalent for mathematical and signal operations (Demo/Assignment only)

# Module 4

# Sampled Data Systems and Z-Transform (9 hours):

Sampling process-Impulse train sampling-sampling theorem- Aliasing effect

Zero order and First order hold circuits- Signal reconstruction

Discrete convolution and its properties

Z Transform: Region of convergence- Properties of Z Transform

Inverse ZT: Methods

# Module 5

# Analysis of Sampled Data Systems (9 hours):

Difference equation representations of LTI systems - Analysis of difference equation of LTI systems- Z Transfer function- Delay operator and block diagram representation-Direct form, cascade and parallel representations of  $2^{nd}$  order systems

Stability of sampled data system: Basic idea on stability- Jury's test- Use of bilinear transformation

Discrete Fourier series: Fourier representation of discrete time signals - Discrete Fourier series- properties.

Discrete Time Fourier Transform: Properties- Frequency response of simple DT systems

# **Text Books**

- 1. Oppenheim A.V., Willsky A.S. & Nawab S.H., Signals and Systems, 2/e, Prentice Hall
- 2. Nagrarth I. J, Saran S. N and Ranjan R, Signals and Systems, 2/e, Tata McGraw Hill
- 3. Haykin S. & Veen B.V., Signals & Systems, 2/e, John Wiley
- 4. Nise N. S., Control Systems Engineering, 6/e, Wiley Eastern
- 5. Nagarath I. J. and Gopal M., Control System Engineering, 5/e, New Age Publishers

# **Reference Books**

- 1. Bracewell R.N., Fourier Transform & Its Applications, McGraw Hill
- 2. Farooq Husain, Signals and Systems, Umesh publications.
- 3. Papoulis A., Fourier Integral & Its Applications, McGraw Hill
- 4. Taylor F.J., Principles of Signals & Systems, McGraw Hill

# **Course Contents and Lecture Schedule:**

Module	Topic coverage	No. of Lectures
1	Introduction to Signals and Systems (9 hours)	
1.1	Classification of signals - Elementary signals- Basic operations on continuous time and discrete time signals	2
1.2	Concept of systems - Classification of systems- Properties of systems - Time invariance- Linearity -Causality – Memory- Stability.	2
1.3	Convolution Integral- Impulse response-	1
1.4	Representation of LTI systems - Differential equation representations of LTI systems	2
1.5	Basics of Non linear systems- types and properties Introduction to random signals and processes (concepts only)	2
2	Fourier Analysis and Laplace Transform Analysis (10 hours)	

	2.1	Fourier Analysis of continuous time signals: Fourier Series- Harmonic analysis of common signals	2
	2.2	Fourier transform: Existence- Properties of Continuous time Fourier transform- Energy spectral density and power spectral density	2
	2.3	Concept of Frequency response- Frequency response of simple LTI systems.	2
	2.4	Laplace transform analysis of system transfer function: Relation between the	1
		transfer function and differential equation	
	2.5	Transfer function of LTI systems: Electrical, Translational and rotational	2
		Mechanical systems	
	2.6	Force Voltage, Force Current and Torque Voltage analogy	1
3		System Models and Response (8 hours)	
	3.1	Block diagram representation - block diagram reduction	2
	3.2	Signal flow graph - Mason's gain formula	1
	3.3	Type and Order of the systems- Characteristic equation.	1
	3.4	Determining the time domain and frequency response from poles and zeros.	2
	3.5	Concepts of Positive real functions and Hurwitz polynomial- Basic idea on	2
		Stability- Routh stability criterion	
	3.6	Simulation based analysis: Introduction to simulation tools like MATLAB/	
		SCILAB or equivalent simulation software and tool boxes for various	
		Solumb of equivalent simulation software and tool boxes for various	
		mathematical operations (Demo/Assignment only)	
4			
4	4.1	mathematical operations (Demo/Assignment only)	2
4	4.1 4.2	mathematical operations (Demo/Assignment only)Sampled Data Systems and Z-Transform (9 hours)	2 2
4		mathematical operations (Demo/Assignment only)Sampled Data Systems and Z-Transform (9 hours)Sampling process-Impulse train sampling-sampling theorem- Aliasing effect	
4	4.2	mathematical operations (Demo/Assignment only)Sampled Data Systems and Z-Transform (9 hours)Sampling process-Impulse train sampling-sampling theorem- Aliasing effectZero order and First order hold circuits- Signal reconstruction-	2
4	4.2 4.3	mathematical operations (Demo/Assignment only)Sampled Data Systems and Z-Transform (9 hours)Sampling process-Impulse train sampling-sampling theorem- Aliasing effectZero order and First order hold circuits- Signal reconstruction-Discrete convolution and its properties	2 1
4	4.2 4.3 4.4	mathematical operations (Demo/Assignment only)Sampled Data Systems and Z-Transform (9 hours)Sampling process-Impulse train sampling-sampling theorem- Aliasing effectZero order and First order hold circuits- Signal reconstruction-Discrete convolution and its propertiesZ Transform: Region of convergence- Properties of Z TransformInverse ZT: MethodsAnalysis of Sampled Data Systems (9 hours)	2 1 2
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	<ul> <li>4.2</li> <li>4.3</li> <li>4.4</li> <li>4.5</li> <li>5.1</li> <li>5.2</li> <li>5.3</li> </ul>	mathematical operations (Demo/Assignment only)Sampled Data Systems and Z-Transform (9 hours)Sampling process-Impulse train sampling-sampling theorem- Aliasing effectZero order and First order hold circuits- Signal reconstruction-Discrete convolution and its propertiesZ Transform: Region of convergence- Properties of Z TransformInverse ZT: MethodsAnalysis of Sampled Data Systems (9 hours)Difference equation representations of LTI systems - Analysis of differenceequation of LTI systems- Z Transfer functionDelay operator and block diagram representation- Direct form, cascade andparallel representations of 2 <sup>nd</sup> order systems.Stability of sampled data system: Basic idea on Stability- Jury's test- Use ofbilinear transformation.	2 1 2 2 2 2 2 2 2
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